9. **Supersymmetry**

9.1 Introduction, concept

9.2 Motivation for SUSY

9.3 Breaking of Supersymmetry

9.4 Supersymmetry pre-LHC

9.5 Search for supersymmetry at the LHC

9.6 How can the parameters of a SUSY model be constrained
Why Physics Beyond the Standard Model?

1. Gravity is not yet incorporated in the Standard Model

2. Dark Matter not accommodated

3. Many open questions in the Standard Model
   - Hierarchy problem: \( m_w \) (100 GeV) \( \rightarrow \) \( m_{\text{Planck}} \) (\( 10^{19} \) GeV)
   - Unification of couplings
   - Flavour / family problem
   - …..

All this calls for a more fundamental theory of which the Standard Model is a low energy approximation \( \rightarrow \) New Physics

Candidate theories: Supersymmetry
Extra Dimensions
……..

Many extensions predict new physics at the TeV scale !!

Strong motivation for LHC, mass reach \(~3\) TeV
9.1 Introduction: what is Supersymmetry (SUSY) ?

SUSY is an extension of the Standard Model (since ~ 1970) that introduces a new symmetry between fermions and bosons:

Spin ½ matter particles (fermions) \[\square\] Spin 1 force particles (bosons)

SUSY transformation (operator Q):

\[Q |\text{Fermion}> \sim |\text{Boson}>\]
\[Q |\text{Boson}> \sim |\text{Fermion}>\]

→ SUSY doubles the number of particles

SUSY is a symmetry, not a theory. A model (a Lagrangian) can possess supersymmetry as a property.
Supersymmetry

Extends the Standard Model by predicting a new symmetry
Spin $\frac{1}{2}$ matter particles (fermions) $\Leftrightarrow$ Spin 1 force carriers (bosons)

Standard Model particles

SUSY particles

Standard Model and supersymmetry partners can be distinguished by a discrete Quantum number: R-parity:

$$ R = (-1)^{3B+L+2S} $$

$ +1$ SM particles

$ -1$ SUSY particles
The SUSY particle spectrum

<table>
<thead>
<tr>
<th>Particle</th>
<th>Sparticle (corresp. SUSY particle)</th>
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<tbody>
<tr>
<td>Spin-1/2</td>
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<tr>
<td>quarks (L&amp;R)</td>
<td></td>
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<tr>
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<td>neutrinos (L)</td>
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<td>Spin-0</td>
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<td><strong>Spin-1</strong></td>
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<td>( B )</td>
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</tr>
<tr>
<td>( W^0 )</td>
<td>( \gamma ) ( Z^0 ) ( W^\pm )</td>
</tr>
<tr>
<td>gluon</td>
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<tr>
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<td>Bino</td>
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<tr>
<td>$W^0$</td>
<td>$Wino^0$</td>
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<tr>
<td>$\gamma$</td>
<td>$Wino^\pm$</td>
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<tr>
<td>$Z^0$</td>
<td>gluino</td>
</tr>
<tr>
<td>$W^\pm$</td>
<td></td>
</tr>
<tr>
<td>gluon</td>
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</tbody>
</table>

Note: Spin refers to the quantum number of a particle, which indicates the particle's behavior under rotations in four-dimensional space-time. Spin-1/2 particles, such as quarks and leptons, do not change their parity under reflections in space-time. Spin-1 particles, such as photons ($\gamma$) and $W^\pm$, change their parity under reflections, while particles with Spin-0, like the Higgs boson and the $Z^0$, do not. Spin-1/2 SUSY particles, such as squarks, sleptons, and sneutrinos, are the supersymmetric counterparts of these ordinary particles.
### Extended Higgs Sector

- **2 complex Higgs doublets**

- **Degrees of freedom:** $8 - 3$ (Goldstone bosons) = **5 Higgs bosons:** $h^0, H^0, A^0, H^\pm$
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</tr>
<tr>
<td>B</td>
<td>Bino</td>
</tr>
<tr>
<td>W^0</td>
<td>Wino^0</td>
</tr>
<tr>
<td>γ</td>
<td>Wino^±</td>
</tr>
<tr>
<td>Z^0</td>
<td>gluino</td>
</tr>
<tr>
<td>W^±</td>
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</tr>
<tr>
<td>gluon</td>
<td></td>
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<td>Higgs</td>
<td>Higgsinos</td>
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<tr>
<td>( H_1^1 )</td>
<td>( \tilde{H}_1^1 )</td>
</tr>
<tr>
<td>( H_2^1 )</td>
<td>( \tilde{H}_2^1 )</td>
</tr>
<tr>
<td>( H_1^2 )</td>
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</tr>
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<td>( \tilde{H}_2^2 )</td>
</tr>
</tbody>
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Extended Higgs sector: 2 complex Higgs doublets

→ Degrees of freedom: 8 - 3 (Goldstone bosons) = 5 Higgs bosons: \( h^0, H^0, A^0, H^\pm \)
Extended Higgs sector: 2 complex Higgs doublets

→ Degrees of freedom: 8 - 3 (Goldstone bosons) = 5 Higgs bosons: $h^0, H^0, A^0, H^\pm$
Extended Higgs sector: 2 complex Higgs doublets

→ Degrees of freedom: 8 - 3 (Goldstone bosons) = 5 Higgs bosons: $h^0, H^0, A^0, H^\pm$

### Particle

| Spin-1/2 | | Spin-0 |
|----------| |        |
| quarks (L&R) | leptons (L&R) | neutrinos (L) |
| squarks (L&R) | sleptons (L&R) | sneutrinos (L) |

### Sparticle (corresp. SUSY particle)

| Spin-1 | | Spin-1/2 |
|---------| |          |
| $B$ | $W^0$ | $\gamma$ |
| $Z^0$ | $W^\pm$ | $\text{gluon}$ |

After Mixing

- 4 neutralinos
- 2 charginos
• Physical neutralinos and charginos are mixtures of Wino, Bino, Higgsinos

• Charginos:

\[
\begin{pmatrix}
\chi_1^+ \\
\chi_2^+
\end{pmatrix} = \begin{pmatrix}
M_2 & \sqrt{2} m_W \sin \beta \\
\sqrt{2} m_W \cos \beta & \mu
\end{pmatrix} \begin{pmatrix}
\tilde{W}^+ \\
\tilde{H}^+
\end{pmatrix}
\]

• Neutralinos:

\[
\begin{pmatrix}
\chi_1^0 \\
\chi_2^0 \\
\chi_3^0 \\
\chi_4^0
\end{pmatrix} = \begin{pmatrix}
M_1 & 0 & -m_Z c_\beta s_W & m_Z s_\beta s_W \\
0 & M_2 & m_Z c_\beta c_W & -m_Z s_\beta c_W \\
-m_Z c_\beta s_W & m_Z c_\beta c_W & 0 & -\mu \\
m_Z s_\beta s_W & -m_Z s_\beta c_W & -\mu & 0
\end{pmatrix} \begin{pmatrix}
\tilde{B} \\
\tilde{W}^3 \\
\tilde{H}_1^0 \\
\tilde{H}_2^0
\end{pmatrix}
\]

Mass eigenstates depend on:

\[M_1, M_2, \tan \beta, \mu\] SUSY masses and breaking parameters
\[m_Z, \sin^2 \theta_W\] EWSB (mixing: \(B^0, W^0 \rightarrow Z, \gamma\))
Supersymmetric particles carry the same quantum numbers (hypercharge, weak isospin, colour) as the Standard Model partners. That means they have the same interaction vertices.

<table>
<thead>
<tr>
<th>Names</th>
<th>spin 0</th>
<th>spin 1/2</th>
<th>$SU(3)_C$, $SU(2)_L$, $U(1)_Y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>squarks, quarks</td>
<td>$Q$</td>
<td>$(\tilde{u}_L , \tilde{d}_L)$</td>
<td>$(u_L , d_L)$</td>
</tr>
<tr>
<td>($\times 3$ families)</td>
<td>$\tilde{u}$</td>
<td>$\tilde{u}^*_R$</td>
<td>$u_R^\dagger$</td>
</tr>
<tr>
<td></td>
<td>$\tilde{d}$</td>
<td>$\tilde{d}^*_R$</td>
<td>$d_R^\dagger$</td>
</tr>
<tr>
<td>sleptons, leptons</td>
<td>$L$</td>
<td>$(\tilde{\nu} , \tilde{e}_L)$</td>
<td>$(\nu , e_L)$</td>
</tr>
<tr>
<td>($\times 3$ families)</td>
<td>$\tilde{e}$</td>
<td>$\tilde{e}_R^*$</td>
<td>$e_R^\dagger$</td>
</tr>
<tr>
<td>Higgs, higgsinos</td>
<td>$H_u$</td>
<td>$(H_u^+ , H_u^0)$</td>
<td>$(\tilde{H}_u^+ , \tilde{H}_u^0)$</td>
</tr>
<tr>
<td></td>
<td>$H_d$</td>
<td>$(H_d^0 , H_d^-)$</td>
<td>$(\tilde{H}_d^0 , \tilde{H}_d^-)$</td>
</tr>
</tbody>
</table>

Table 1.1: Chiral supermultiplets in the Minimal Supersymmetric Standard Model. The spin-0 fields are complex scalars, and the spin-1/2 fields are left-handed two-component Weyl fermions.
<table>
<thead>
<tr>
<th>Names</th>
<th>spin 1/2</th>
<th>spin 1</th>
<th>$SU(3)_C$, $SU(2)_L$, $U(1)_Y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>gluino, gluon</td>
<td>$\tilde{g}$</td>
<td>$g$</td>
<td>$(8, 1, 0)$</td>
</tr>
<tr>
<td>winos, W bosons</td>
<td>$\tilde{W}^\pm \tilde{W}^0$</td>
<td>$W^\pm W^0$</td>
<td>$(1, 3, 0)$</td>
</tr>
<tr>
<td>bino, B boson</td>
<td>$\tilde{B}^0$</td>
<td>$B^0$</td>
<td>$(1, 1, 0)$</td>
</tr>
</tbody>
</table>

Gauge supermultiplets in the Minimal Supersymmetric Standard Model.
R parity

- New terms in Lagrangian:
  \[ W_{RPV} = \frac{1}{2} (\lambda LLE + \lambda' LQD + \lambda'' UDD) + \mu LH \]

Problem: These couplings lead to proton decay

Unacceptably high rate compared to experimental limits
(proton lifetime > 10\(^{33}\) years)

→ Strong limits on product of couplings

- Introduce multiplicative quantum number:
  \[ R_p = (-1)^{3(B-L)+2S} \]
  = +1 for SM particles
  = -1 for SUSY particles

- Impose \( R_p \) conservation:
  - Sparticles produced in pairs
  - Lightest SUSY particle (LSP) stable
Experimental consequences of R-parity conservation:

• SUSY particles are produced in pairs

• Lightest Supersymmetric Particle (LSP) is stable.

  LSP is only weakly interacting:
  \[ \text{LSP} \equiv \chi^0_1 \text{ (lightest neutralino, in many models)} \]
  \[ \rightarrow \text{LSP behaves like a } \nu \rightarrow \text{it escapes detection} \]
  \[ \rightarrow E_T^{\text{miss}} \text{ (typical SUSY signature)} \]
SUSY interactions, some examples

The coupling constants are the same as in SM (strong, electroweak)

“Recipe” : Obtain SUSY interactions by exchanging
at a vertex two SM legs by corresponding SUSY legs
Sparticle production at the LHC

Quark-gluon fusion

Quark annihilation
9.2 Motivation for supersymmetry

or what problems of the Standard Model does it solve?
(i) The Hierarchy or naturalness problem

- In the Standard Model, quadratically divergent quantum corrections to the Higgs mass appear

\[ \Delta m_H^2 = -\frac{|\lambda_f|^2}{8\pi^2} \Lambda_{UV}^2 + \ldots \]

- The symmetry between bosons and fermions, which contribute with different sign (statistics), can cure this problem:

\[ \Delta m_H^2 = \frac{\lambda_s}{16\pi^2} \left[ \Lambda_{UV}^2 - 2m_S^2 \ln(\Lambda_{UV}/m_S) + \ldots \right] \]

\[ \Delta m_H = f(m_B^2 - m_f^2) \]

→ terms cancel one-by-one if SUSY were a perfect symmetry (i.e. if \( m(\text{particle}) = m(\text{sparticle}) \)). Since this is not the case, sparticles should not be too heavy (\( m_{\text{SUSY}} \sim 1 \text{ TeV} \)).
(ii) The unification of the couplings of the three interactions seems possible in a SUSY model.

Due to quantum corrections, e.g. slope is changed due to contributions from SUSY particles.
(ii) SUSY provides a candidate for the Dark Matter in the universe

Evidence from:

- Rotational curves of galaxies
- Gravitational lensing
- Cosmic microwave background (CMB)
Dark-Matter properties:

- Gravitationally interacting

- Not short-lived
- Not hot
- Not baryonic, no el. magnetic interaction

→ Unambiguous evidence for new physics!
• SUSY has a **weakly interacting massive particle (WIMP)**, if R-parity is conserved:
  
  the lightest supersymmetric particle

• **LSP** = lightest neutralino, gravitino (depending on SUSY model)
9.3 Breaking of Supersymmetry

- or the dark side of SUSY -
• **Supersymmetry cannot be an exact symmetry**, since we have not seen SUSY particles with masses equal to the Standard Model particles (e.g. no scalar electrons with masses of 511 keV)

• It is expected that supersymmetry is **broken spontaneously**, i.e. the underlying model should have a Lagrangian density that is invariant under supersymmetry, but a vacuum state that is not.

• **The mechanism of SUSY breaking is not known**

• Our ignorance is parametrized by introducing extra terms that break SUSY explicitly (so called soft SUSY breaking terms*) into the Lagrangian and consider it as an “effective” Lagrangian

• → about 105 parameters are introduced: masses, couplings, mixing angles…..

*) only such terms are allowed that guarantee that no new quadratically divergent radiative corrections appear
A general parametrization comprises:

- Scalar mass terms: \( m_i^2 \phi_i^2 \)
- Gaugino mass terms: \( \frac{1}{2} M_a V'_a C V_a \)
- Coupling terms of scalar particles: \( A_\lambda \lambda \phi^3 \), \( B_\mu \mu \phi^2 \)

It is often assumed that these supersymmetry breaking terms originate at some high scale (Grand Unification scale (GUT scale), or gravity scale).... maybe linked to some supergravity or superstring mechanism.

It is furthermore often assumed that the soft supersymmetry-breaking terms are universal at the GUT or supergravity scale.
The Minimal Supersymmetric Extension to the SM (MSSM)

It includes 105 additional parameters on top of the SM ones:

- SUSY violating mass terms for each partner of the SM fermions
- SUSY violating mass terms for each partner of the SM bosons
- Additional parameters on the Higgs sector (5 Higgs bosons in total)
- Trilinear couplings of all scalar particles

These parameters cannot be all independent:

- Or we would have large FCNC, CP violation, etc.
- Consistency with existing measurements indicate some ordering principle is at play
Bottom up approach - The phenomenological MSSM (pMSSM)

- Reasonable assumptions (motivated by current experimental results):
  - The mass matrices are diagonal and proportional to the identity matrix (no FCNC)
  - The trilinear couplings are proportional to the Yukawa couplings
  - No additional complex phase in the matrices (no additional CP violation)
  - Unified masses of first and second sfermions generations (from $K^0$-anti-$K^0$ mixing)

Then one ends up with the so-called phenomenological MSSM, which has 19 parameters in addition to the SM parameters

\[ \tan \beta : \text{the ratio of the vev of the two-Higgs doublet fields.} \]
\[ M_A : \text{the mass of the pseudoscalar Higgs boson} \]
\[ \mu : \text{the Higgs-higgsino mass parameter} \]
\[ M_1, M_2, M_3 : \text{the bino, wino and gluino mass parameters.} \]
\[ m_q, m_{\tilde{e}_R}, m_{\tilde{\ell}_R}, m_{\tilde{\ell}_L}, m_{\tilde{\tau}_R} : \text{first/second generation sfermion masses} \]
\[ m_Q, m_{\tilde{t}_R}, m_{\tilde{b}_R}, m_{\tilde{\ell}_L}, m_{\tilde{\tau}_R} : \text{third generation sfermion masses} \]
\[ A_t, A_b, A_\tau : \text{third generation trilinear couplings.} \]
Top-down approaches: Constrained MSSM models

It is often assumed that these supersymmetry breaking terms originate at some high scale (Grand Unification scale (GUT scale), or gravity scale) …. maybe linked to some supergravity or superstring mechanism

It is furthermore often assumed that the soft supersymmetry-breaking terms are universal at the GUT or supergravity scale

The constrained MSSM models make strong assumptions about unification of SUSY parameters. They have been very popular for many years

But they really suffer from the LHC constraints….. With time, they are becoming less and less popular
If one assumes universality for all masses and couplings at the GUT scale, the following five parameters suffice to characterize the MSSM (Minimal Supersymmetric Standard Model)

**Five parameters:**

- $m_0 =$ common sfermion mass at the GUT scale
- $m_{1/2} = M_1 = M_2$ (common gaugino mass at the GUT scale)
- $A_0$ common coupling term
- $\tan \beta$ ratio of vacuum expectation value of the two Higgs doublets
- $\mu$ Higgs mass term

The parameters $\mu$ and $\tan \beta$ are related to the Higgs sector of the MSSM and determine this sector –together with one Higgs boson mass, e.g. $m_A$ - at tree level completely.

This model is referred to as “constrained MSSM”
The energy dependence of the SUSY particle masses can be calculated (renormalization group equations).

- In such models, squarks and/or gluinos are the heaviest sparticles.
- Stops might be the lightest squarks.
- Mixing effects (see later) can lead to mass splitting between \( t_L \) and \( t_R \).
- Sleptons / charginos / neutralinos are lightest sparticles.

In this example separate Higgs boson mass terms are used at the GUT scale.
Example for a calculated mass spectrum at the electroweak scale:

- In many models, the lightest neutralino is the lightest SUSY particle (LSP)
- Lightest Higgs boson ($h^0$) might also be light, split from heavier Higgs particles
- Production of SUSY particles at the LHC is dominated by coloured squarks and gluinos
SUSY mass spectra for different SUSY breaking models:

- **mSUGRA**: minimal SUperGRAvity model (gravity responsible for SUSY breaking)
- **GMSB**: Gauge mediated SUSY Breaking (breaking via gauge interactions)
- **AMSB**: Anomaly mediated SUSY Breaking

mSUGRA: minimal SUperGRAvity model (gravity responsible for SUSY breaking)
GMSB: Gauge mediated SUSY Breaking (breaking via gauge interactions)
AMSB: Anomaly mediated SUSY Breaking
Sparticle Masses and Mixing

(i) Sfermions:

• Each flavour of charged leptons or quarks has both left- and right handed components, $f_{L,R}$ and these have separate spin-0 boson superpartners $f'_{LR}$.

• The superpartners can mix, and the mass matrix in MSSM is given by:

$$M_f^2 = \begin{pmatrix}
    m_{f_{LL}}^2 & m_{f_{LR}}^2 \\
    m_{f_{LR}}^2 & m_{f_{RR}}^2
  \end{pmatrix}$$

where the off-diagonal mixing terms take the general form (with $m_f$ being the corresponding fermion mass).

$$m_{f_{L,R}}^2 = m_f \left( A_f + \mu \cot \beta \right) \quad \text{for} \quad f = e, \mu, \tau, d, s, b$$

• Since mixing effects are proportional to the SM fermion masses, they are in particular important for third generation sfermions. They are as well enhanced for large $\tan \beta$.

• Diagonalization of this mass matrix leads to the physical SUSY particle masses. Mixing might split the two states in mass, usually referred to as the lighter $f'_{1}$ and the heavier state $f'_{2}$. 
Sparticle Masses and Mixing

(ii) Charginos:

- Charginos are the supersymmetric partners of the $W^\pm$ and charged Higgs bosons $H^\pm$.

Their masses are determined via the parameters: $M_2$, $\mu$ and $\tan \beta$ appearing in the mass mixing matrix $M_{C}$:

$$-\frac{1}{2} \begin{pmatrix} \tilde{W}^- \, \tilde{H}^- \end{pmatrix} M_{C} \begin{pmatrix} \tilde{W}^+ \\ \tilde{H}^+ \end{pmatrix} + \text{herm.conj.}$$

$$M_{C} \equiv \begin{pmatrix} M_2 & \sqrt{2}m_{W} \sin \beta \\ \sqrt{2}m_{W} \cos \beta & \mu \end{pmatrix}$$

where $M_2$ is the unmixed SU(2) gaugino mass and $\mu$ is the Higgs mass parameter.
Sparticle Masses and Mixing

(ii) Neutralinos:

- Masses of neutralinos, the supersymmetric partners of the neutral fields $(\tilde{W}^3, \tilde{B}, \tilde{H}_2^0, \tilde{H}_1^0)$

are given by the following mixing matrix:

$$m_N = \begin{pmatrix}
M_2 & 0 & \frac{-g_2 v_2}{\sqrt{2}} & \frac{g_2 v_1}{\sqrt{2}} \\
0 & M_1 & \frac{g' v_2}{\sqrt{2}} & \frac{-g' v_1}{\sqrt{2}} \\
\frac{-g_2 v_2}{\sqrt{2}} & \frac{g' v_2}{\sqrt{2}} & 0 & \mu \\
\frac{g_2 v_1}{\sqrt{2}} & \frac{-g' v_1}{\sqrt{2}} & \mu & 0
\end{pmatrix}$$

where $M_1, M_2$ is the unmixed U(1), SU(2) gaugino mass, $\mu$ is the Higgs mass parameter, and $g_2$ and $g'$ are the gauge couplings of the SU(2) / U(1) group.
Because of the large top Yukawa coupling, the Higgs boson and the stop sector turn out to be heavily connected

\[ m_h^2 = m_Z^2 \cos^2 \beta + \frac{3y_t^2m_t^2}{(4\pi)^2} \left[ \log \left( \frac{m_S^2}{m_t^2} \right) + X_t^2 \left( 1 - \frac{X_t^2}{12} \right) \right] + \cdots \]

The natural Higgs mass is \( m_Z \). However, loop corrections are large.

\[ X_t = (A_t - \frac{\mu}{\tan \beta}) \]

\[ M_S = \frac{1}{m_{t_1} m_{t_2}} \]

\[ M_t^2 = \begin{pmatrix}
  m_Q^2 + m_t^2 & m_t(A_t - \mu^*/\tan \beta) \\
  m_t(A_t^* - \mu/\tan \beta) & m_U^2 + m_t^2
\end{pmatrix} \]
Link to the Dark Matter in the Universe?

Parameters of the SUSY model $\Rightarrow$ predictions for the relic density of dark matter

Interpretation in a simplified model

cMSSM
(constrained Minimal Supersymmetric Standard Model)

Five parameters:
- $m_0, m_{1/2}$ particle masses at the GUT scale
- $A_0$ common coupling term
- $\tan \beta$ ratio of vacuum expectation value of the two Higgs doublets
- $\mu$ (sign $\mu$) Higgs mass term

regions of parameter space which are consistent with the measured relic density of dark matter (WMAP,.....)
9.4 Supersymmetry pre-LHC

9.4.1 SUSY searches at LEP

9.4.2 SUSY searches at the Tevatron
Indirect SUSY searches

- Measure branching fractions of rare decays or search for forbidden decays. → Potentially enhanced by SUSY particles “in loops”:

- Measurement of anomalous magnetic moment ($g-2$): Brookhaven
Direct searches – general approach

- R-parity conserving Supersymmetry means **missing transverse momentum** in the final state

The simplest possible search strategy:
- A harsh cut on the missing transverse momentum will strongly reduce the number of expected events from known Standard Model Processes

→ Search for excess in high $E_T^{\text{miss}}$ region
Direct searches – limit settings

- What if instead the number of observed events is consistent with the SM prediction?

- For a given signal hypothesis, one can compute if the number of expected (observed) SM events differs from the expected (observed) SM + SUSY yield for more than 2 Gaussian equivalent sigmas

If yes, the model is excluded (either expected to be excluded or excluded)
Direct searches for sleptons at LEP

• Clear domain of LEP are Slepton & Chargino/Neutralino searches (e^+e^-, E_{cm} ~ 200 GeV)

→ Excluded up to masses of 80 ... 100 GeV (~ E_{cm}/2)

\[ \tilde{\ell} \rightarrow \ell \chi^0_1 \] (2 leptons + missing E)

OPAL stau event candidate
Direct searches for charginos at LEP

Large $m_0$ ($\tilde{\ell}$ are heavy)

$$\gamma, Z^* \rightarrow \chi^+ \chi^- \rightarrow W^* \chi_1^0 W^* \chi_1^0$$

Small $m_0$ ($\tilde{\ell}$ are light)

$$\chi^+ \chi^- \rightarrow \ell^+ \tilde{\nu} \ell^- \tilde{\nu} \rightarrow \ell^+ \nu \chi_1^0 \ell^- \nu \chi_1^0$$

Main SM backgrounds (WW, ZZ production) suppressed by requiring large missing mass or missing energy in the event.
The two classical SUSY signatures at the Tevatron

1. Search for Squarks and Gluinos: \( \text{Jet} + E_T^{\text{miss}} \) signature
   produced via QCD processes

   \[ \tilde{\chi}_2 \tilde{\chi}_1 \rightarrow l^\pm l'^\mp \tilde{\chi}_1 \tilde{\chi}_1 X \]

2. Search for Charginos and Neutralinos: \( \text{Multilepton} + E_T^{\text{miss}} \) signature
   produced via electroweak processes (associated production – not discussed here)
Search for Squarks and Gluinos

• Three different analyses, depending on squark / gluinos mass relations:

(i) dijet analysis
   small $m_0$, $m(\text{squark}) < m(\text{gluino})$

(ii) 3-jet analysis
   intermediate $m_0$ $m(\text{squark}) \approx m(\text{gluino})$

(iii) Gluino analysis
   large $m_0$, $m(\text{squark}) > m(\text{gluino})$

• Main backgrounds: $Z \rightarrow \nu\nu + \text{jets}$, $tt$, $W + \text{jet production}$

• Event selection:
  * require at least 2, 3 or 4 jets with $P_T > 60 / 40 / 30 / 20$ GeV
  * veto on isolated electrons and muons
  * isolation of $E_T^{\text{miss}}$ and all jets
  * optimization of the final cuts $\rightarrow$ discriminating variables
Search for Squarks and Gluinos (cont.)

No excess above background from Standard Model processes
→ No evidence for SUSY (yet) → Set limits on masses of SUSY particles

**Expected background:**

<table>
<thead>
<tr>
<th>samples</th>
<th>2-jets</th>
<th>3-jets</th>
<th>4-jets</th>
</tr>
</thead>
<tbody>
<tr>
<td>QCD</td>
<td>4.37±2.01</td>
<td>13.34±4.67</td>
<td>15.26±7.60</td>
</tr>
<tr>
<td>top</td>
<td>1.35±1.22</td>
<td>7.56±3.85</td>
<td>22.14±7.29</td>
</tr>
<tr>
<td>Z→νν+jets</td>
<td>3.95±1.09</td>
<td>5.39±1.74</td>
<td>2.74±0.95</td>
</tr>
<tr>
<td>Z→ll+jets</td>
<td>0.09±0.04</td>
<td>0.16±0.11</td>
<td>0.14±0.08</td>
</tr>
<tr>
<td>W→ℓν+jets</td>
<td>6.08±2.15</td>
<td>10.69±3.84</td>
<td>7.68±2.85</td>
</tr>
<tr>
<td>WW/WZ/ZZ</td>
<td>0.21±0.19</td>
<td>0.33±0.17</td>
<td>0.49±0.34</td>
</tr>
<tr>
<td>tot SM</td>
<td>16±5</td>
<td>37±12</td>
<td>48±17</td>
</tr>
</tbody>
</table>

**Observed events in data:**

<table>
<thead>
<tr>
<th>Region</th>
<th>Observed data</th>
</tr>
</thead>
<tbody>
<tr>
<td>4-jets</td>
<td>45</td>
</tr>
<tr>
<td>3-jets</td>
<td>38</td>
</tr>
<tr>
<td>2-jets</td>
<td>18</td>
</tr>
</tbody>
</table>
Excluded regions in the m(squark) vs. m(gluino) plane

**Exclusion limits**
(incl. systematic uncertainties)*:

- m(gluino) > 290 GeV/c²
- m(squark) > 375 GeV/c²

*) uncertainties from structure functions, change of renormalization and factorization scale $\mu$ by a factor of 2, NLO calculation, default choice: $\mu = m(\text{gluino})$, m(squark) or $\frac{1}{2}(m(\text{gluino})+m(\text{squark}))$ for gg, qq, qg production
Search for Charginos and Neutralinos - the tri-lepton channel-

- Gaugino pair production via electroweak processes (small cross sections, ~0.1 – 0.5 pb, however, small expected background)

- For small gaugino masses (~100 GeV/c²) one needs to be sensitive to low Pₜ lepton
Analysis:

- Search for different $(\ell\ell\ell) + \text{like-sign } \mu\mu$ final states with missing transverse momentum
- In order to gain efficiency, no lepton identification is required for the 3rd lepton, select: two identified leptons + a track with $p_T > 4 \text{ GeV/c}$

For specific scenarios: sensitivity / limits above LEP limits; e.g., $M(\chi^\pm) > 140 \text{ GeV/c}^2$ for the 3l-max scenario